Myopically Verifiable Probabilistic Certificate for Long-term Safety

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理学

Stochastic safe control Robust control Optimization Information theory ...





Neuroscience Biomolecular control...



工学

Today's talk

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Safety is critical for intelligent systems







Autonomous vehicles

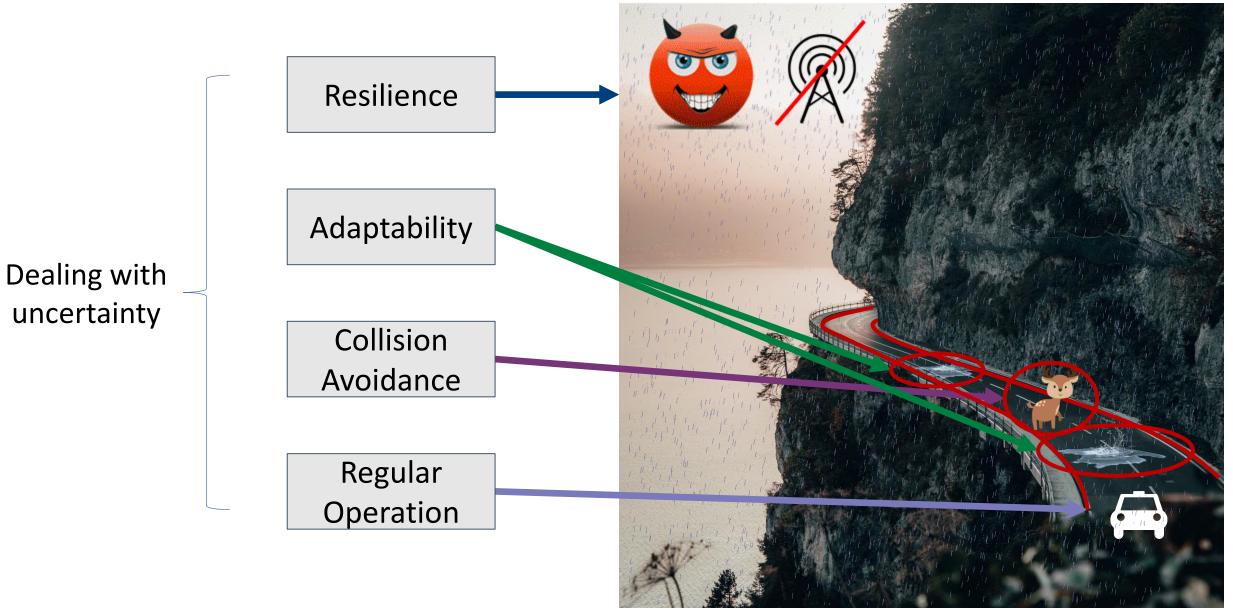
Cobots Intelligent manufacturing

Drones

Safety is critical for intelligent systems

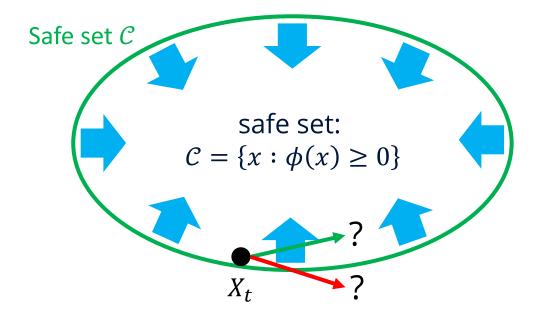


Safety is critical for intelligent systems



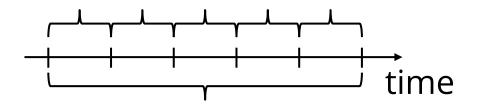
Challenges: achieving safety in uncertainty

Existing approach: Control barrier function...



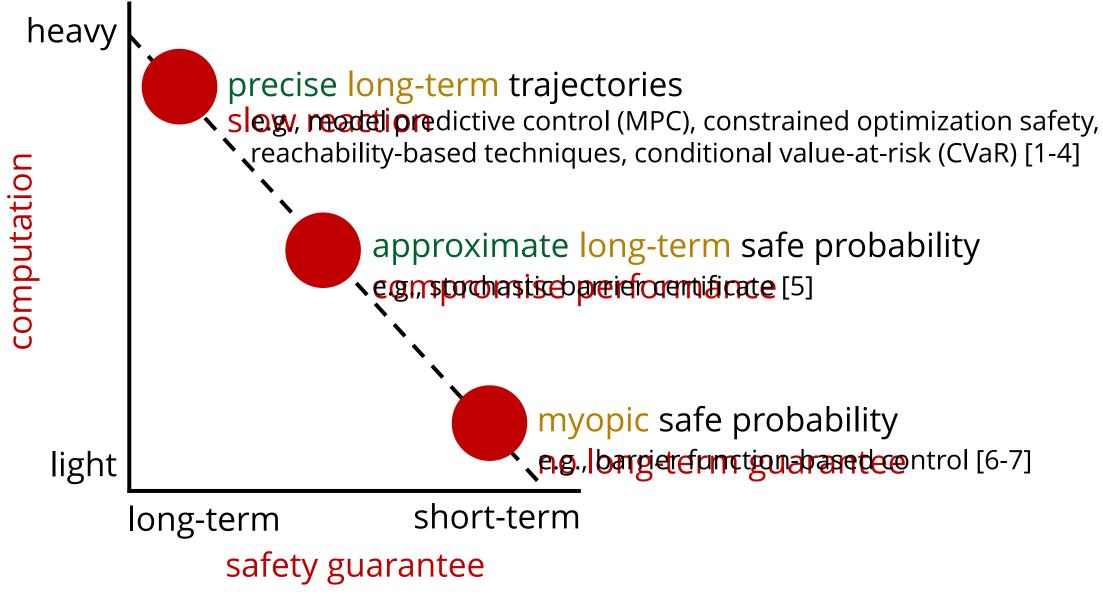
Under stochastic uncertainties safe at next time => safe at all time

safe with probability $1 - \delta$ at each step



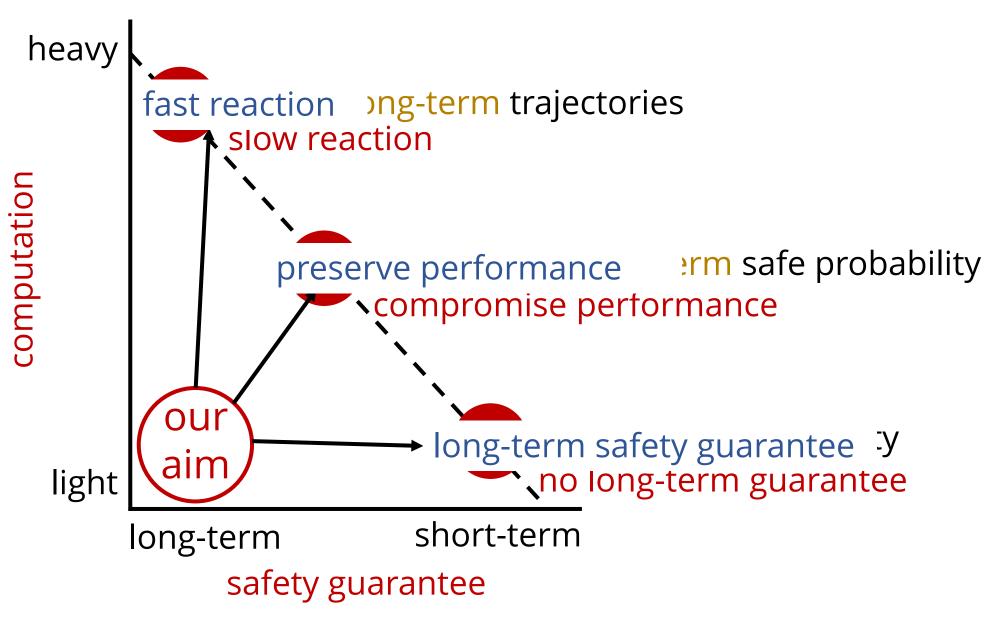
unsafe with high probability in a long term

Current Challenges

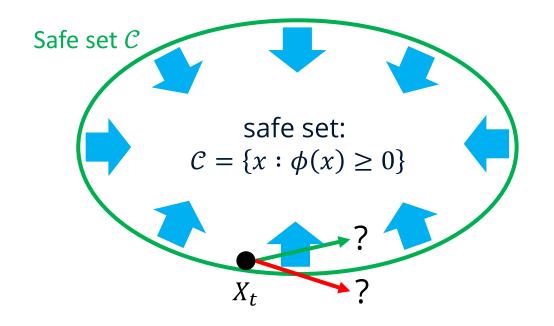


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Aims

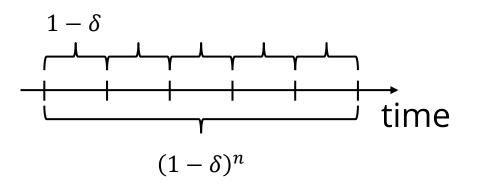


Existing approach: Control barrier function...



Under stochastic uncertainties safe at next time => safe at all time

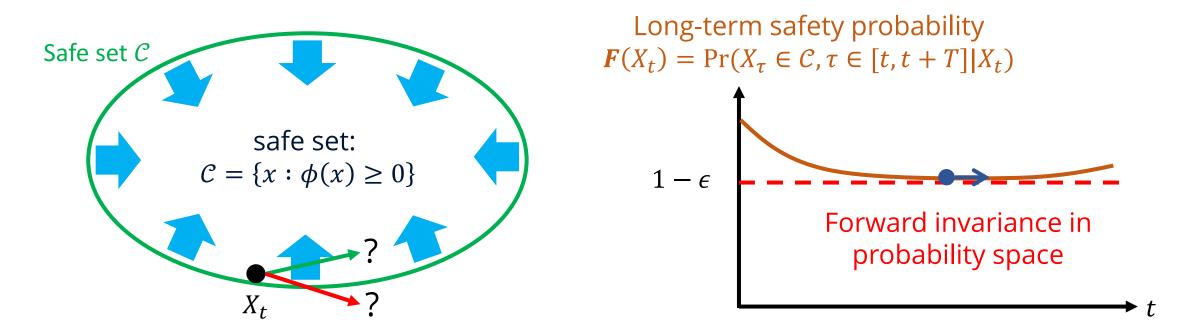
safe with probability $1 - \delta$ at each step



unsafe with high probability in a long term

Existing approach: Control barrier function...

Proposed approach:



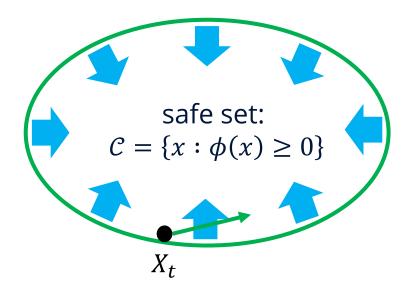
Under stochastic uncertainties

Control barrier functions:

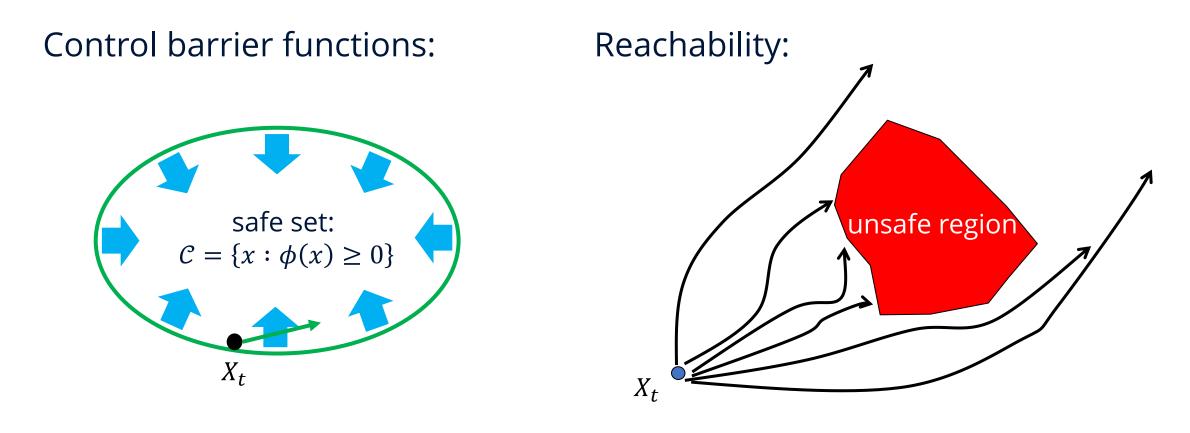
Reachability:

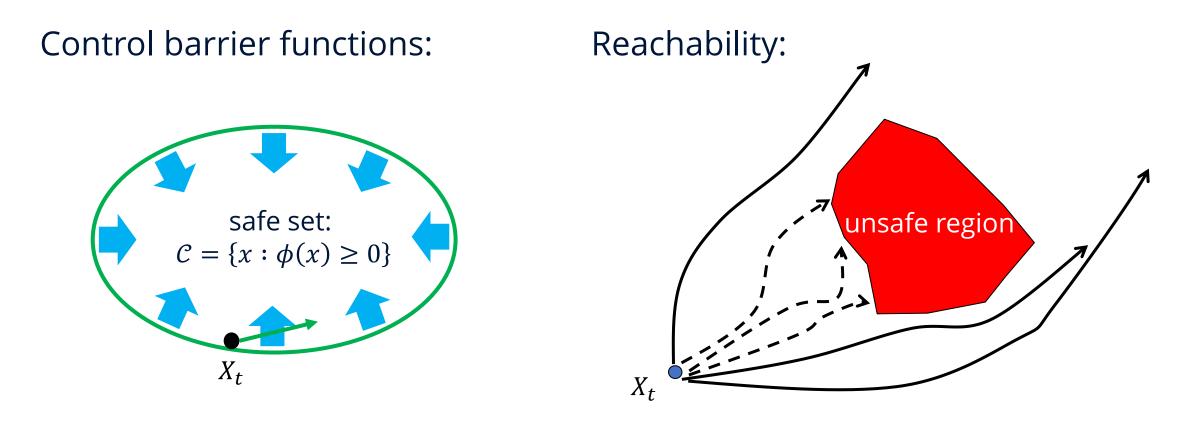
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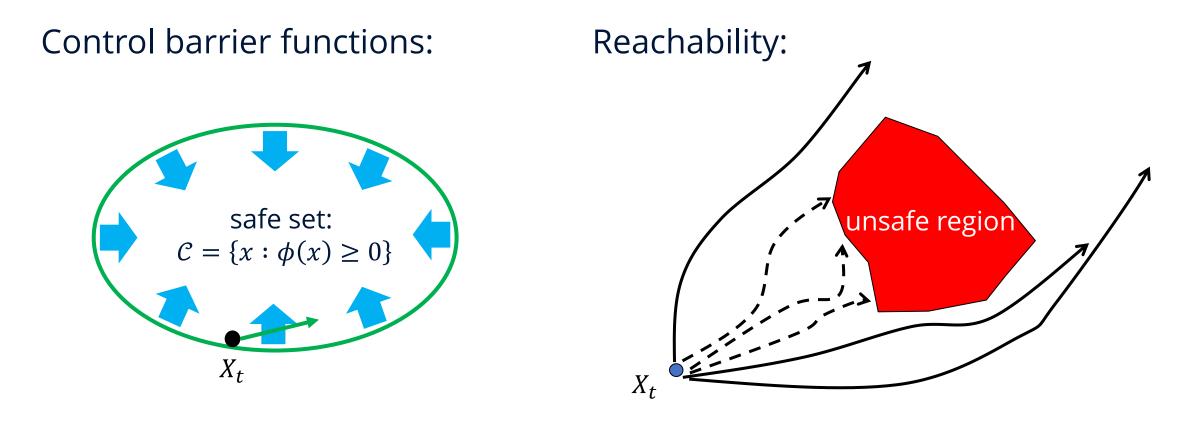
 X_t



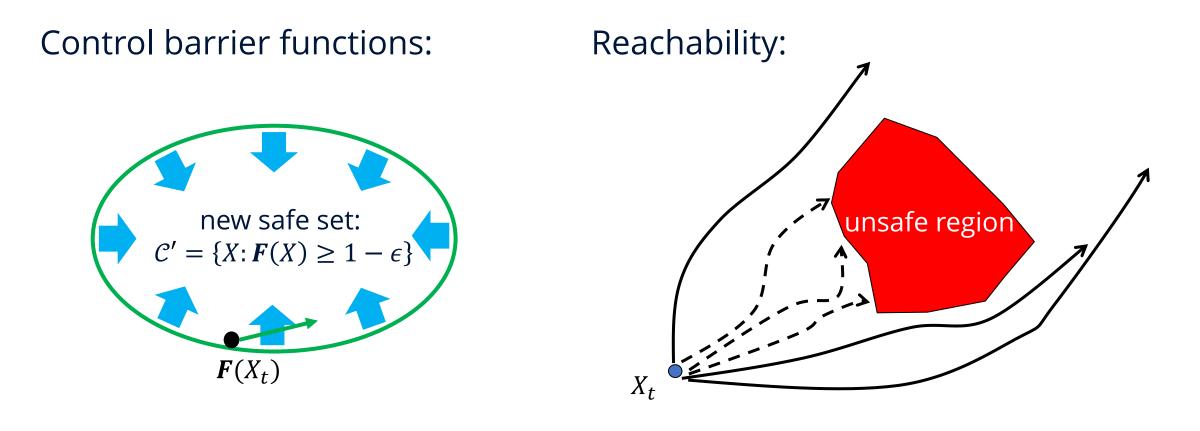




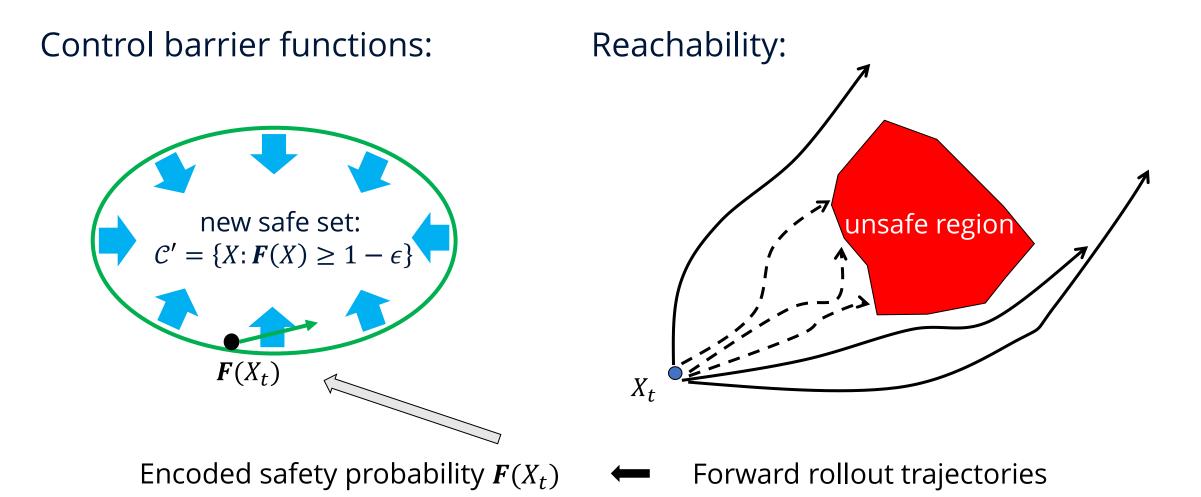




Encoded safety probability $F(X_t)$

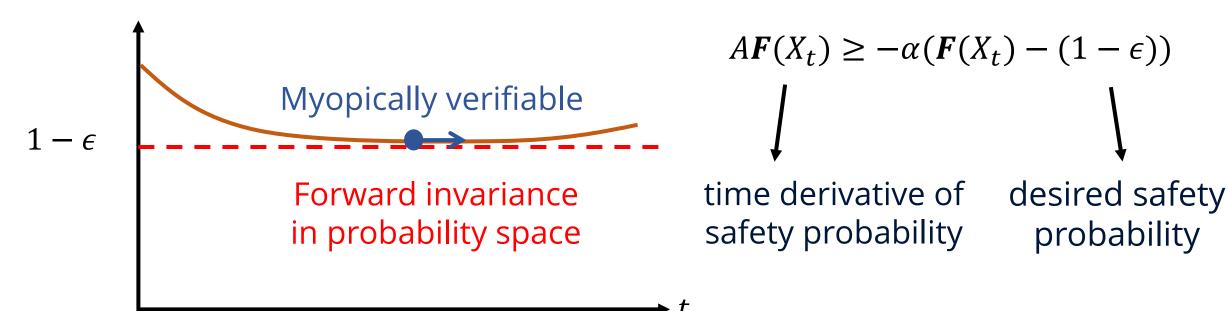


Encoded safety probability $F(X_t)$



Proposed Method

Long-term safe probability $F(X_t) = \Pr(X_\tau \in C, \tau \in [t, t + T] | X_t)$



Proposed Safety Condition:

A: infinitesimal generator $\alpha: \mathbb{R} \to \mathbb{R}$ monotonically increasing, concave, $\alpha(0) \leq 0$.

Theoretical Guarantees

Theorem: Given

$$F(X_0) > 1 - \epsilon,$$

if we choose the control action to satisfy

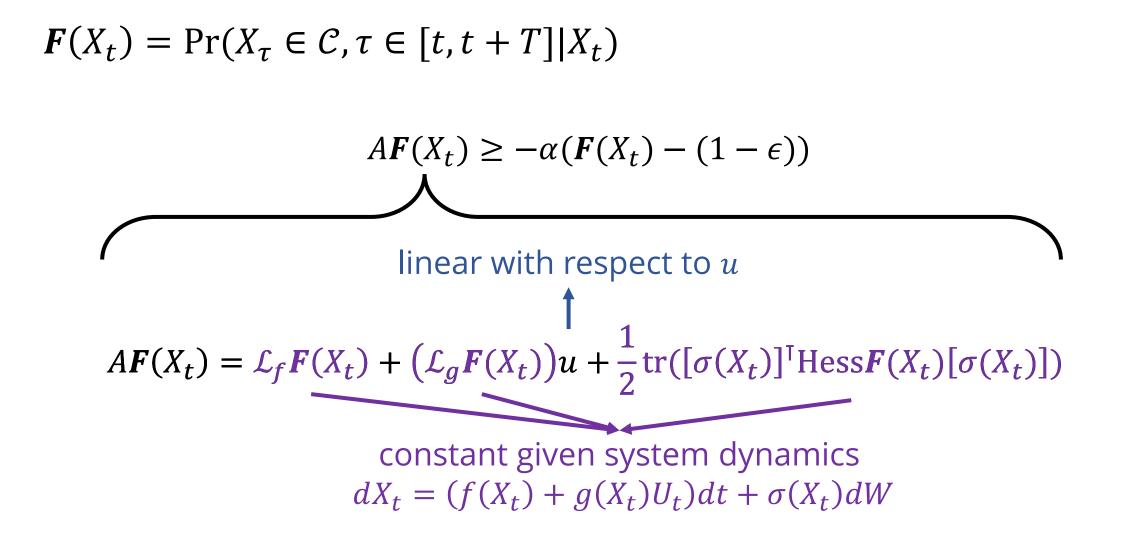
$$A\mathbf{F}(X_t) \ge -\alpha(\mathbf{F}(X_t) - (1 - \epsilon))$$
 for $t > 0$

then we have

$$\Pr(X_{\tau} \in \mathcal{C}, \tau \in [t, t + T]) \ge 1 - \epsilon \text{ for } \forall t > 0$$

 $\alpha: \mathbb{R} \to \mathbb{R}$ is a monotonically increasing concave function that satisfies $\alpha(0) \leq 0$.

Proposed Safety Condition



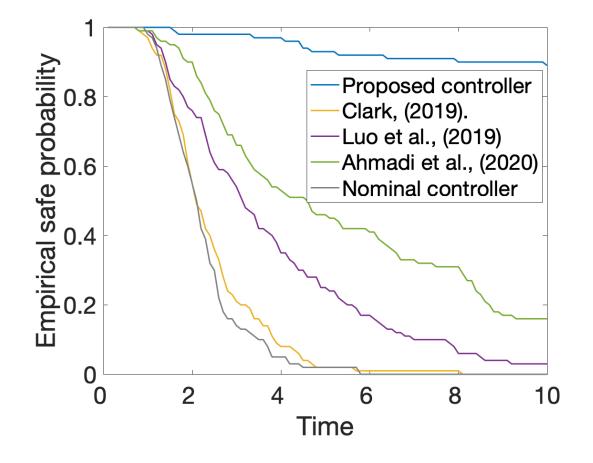
Simulation

system dynamic:	$dx_t = (2x_t + 2.5u_t) dt + 2dw_t$
initial state:	$x_0 = 3$
safe set:	$\mathcal{C} = \{ x \in \mathbb{R} : x - 1 > 0 \}$
nominal controller:	$N(x_t) = 2.5x_t$
desired safety probability:	$1 - \epsilon = 0.9$

Simulation

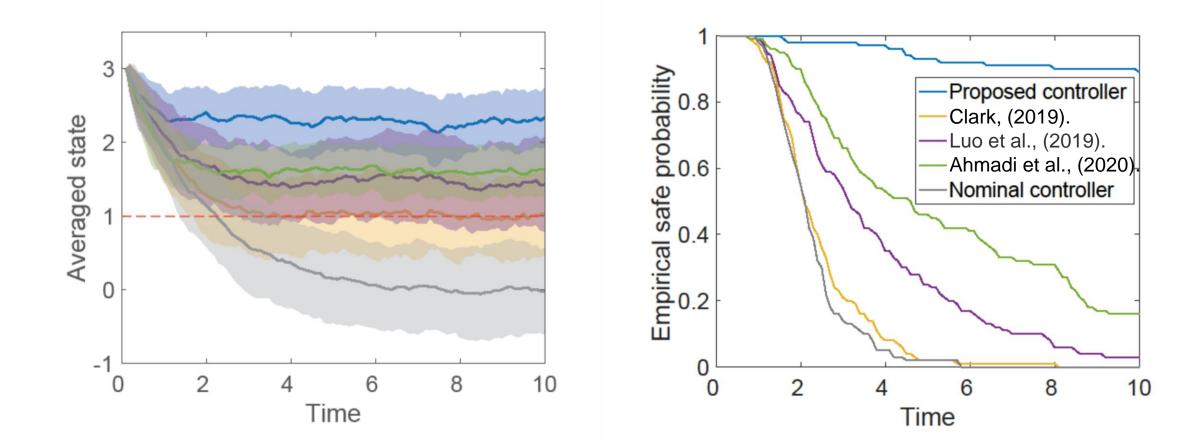
Empirical safety probability:

Safety conditions:



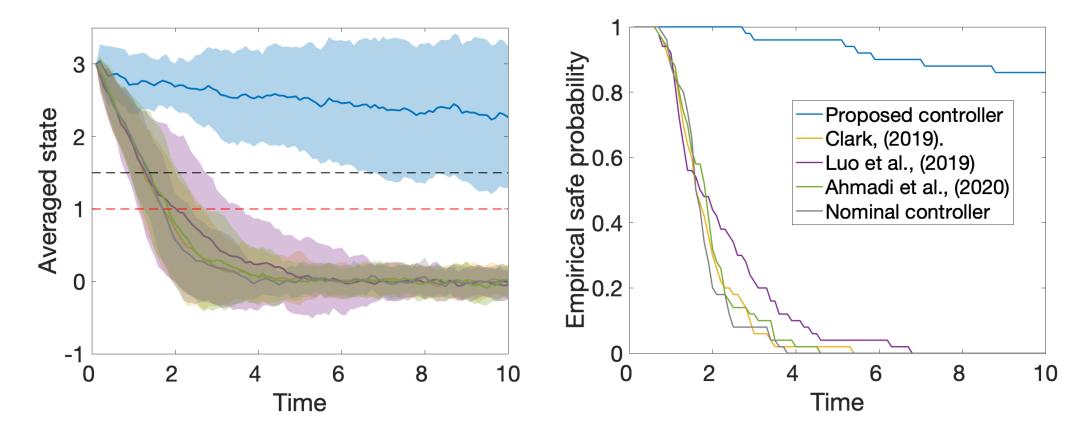
Proposed: $AF(X_t) \ge -\alpha(F(X_t) - (1 - \epsilon))$ Clark: $A\phi(X_t) \ge -\alpha\phi(X_t)$ Luo et al.: $\mathbb{P}(d\phi(X_t, U_t) + \alpha\phi(X_t) \ge 0) \ge 1 - \epsilon$ Ahmadi et al.: $CVaR_{\beta}(\phi(X_{t+1})) \ge \gamma\phi(X_t)$

Simulation



Simulation – Nonlinear trap

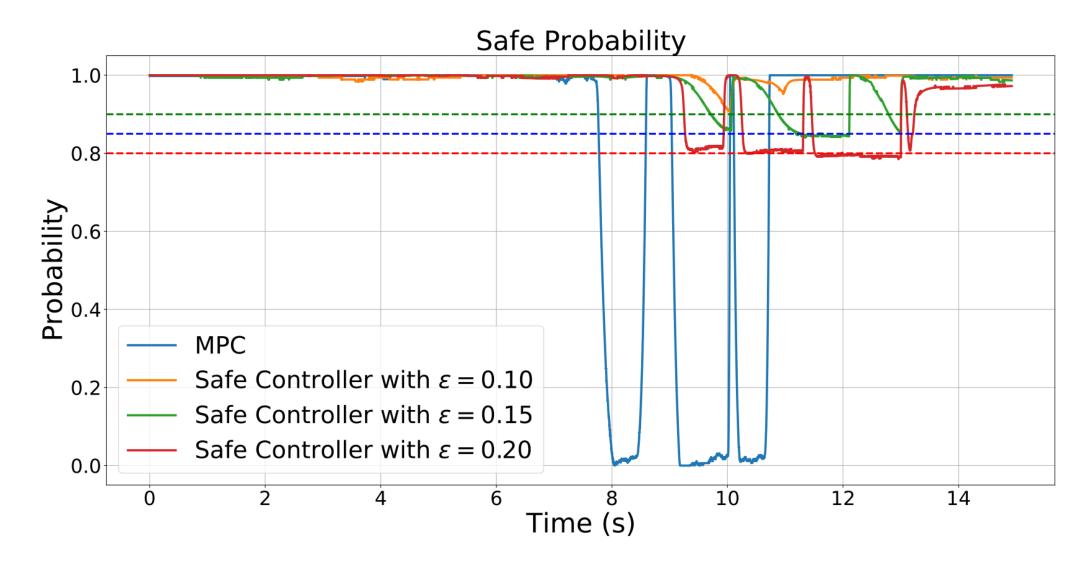
System becomes uncontrollable once reach state x = 1.5



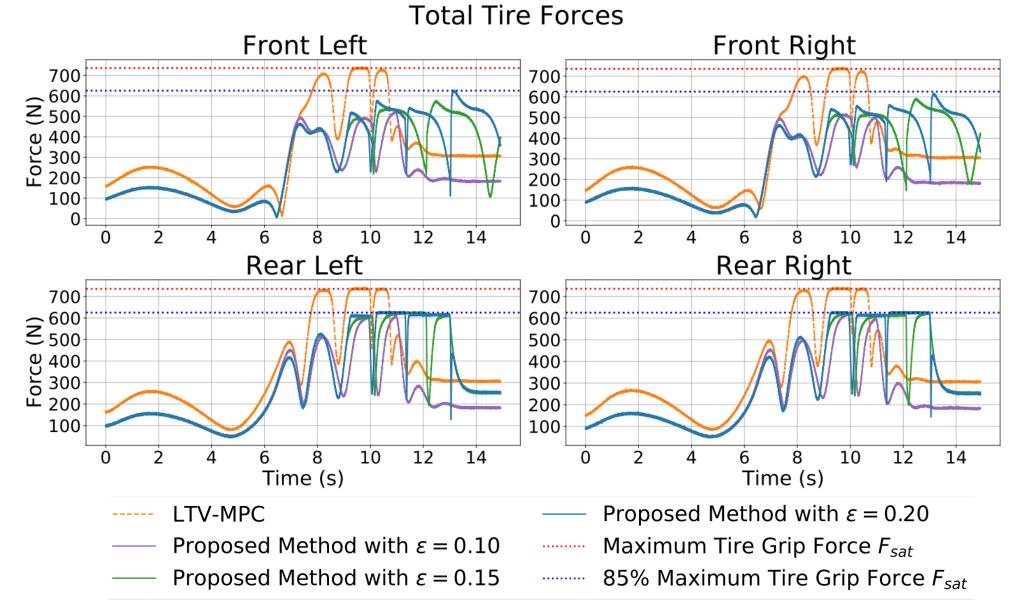
Setting: vehicle slippery -> lose of control -> loss of safety



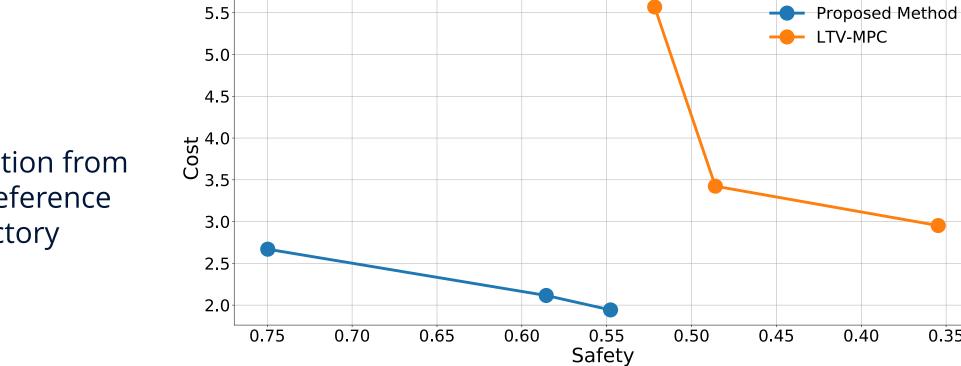
Advantage 1: Long-term Safety Guarantee



Advantage 1: Long-term Safety Guarantee (Cont'd)



Advantage 2: Better Performance Tradeoffs



deviation from the reference trajectory

cost:

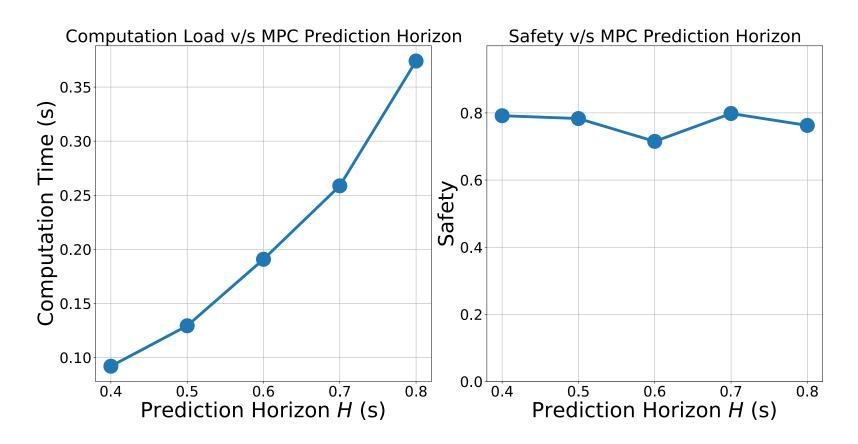
safety: satisfaction of the tire force limits

0.35

Safety v/s Performance

Advantage 3: Less Computation Costs

- Computation of MPC grows in $O(H^3)$
- Safety will not be compromised even with short outlook horizons



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Microfinance from a control perspective

• Microfinance in developing areas has been proven to improve the local economy significantly.

However, building reliable microfinance system is challenging

- 1. Complexity in understanding default process
- 2. Asymmetry, heterogeneity, and incomplete information of individual applications
- 3. The scarcity of available past data
- 4. The dynamically evolving social and economic conditions

Features of Proposed Algorithm:

Benefit in Microfinance

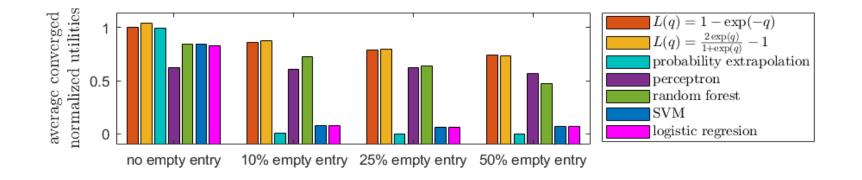
Information	Exploration	Initial Learning Stage	Proactive Policy Design	Steady Stage
Gathering		Provide financial opportunities		Adapt to changing economic & social situations
Policy Objective			Design new policies with - Group association	
Optimized Decision	Exploitation	Find reliable loan policies Sustainability Concern		Optimize social welfare Financial Inclusion

Technical Enablers

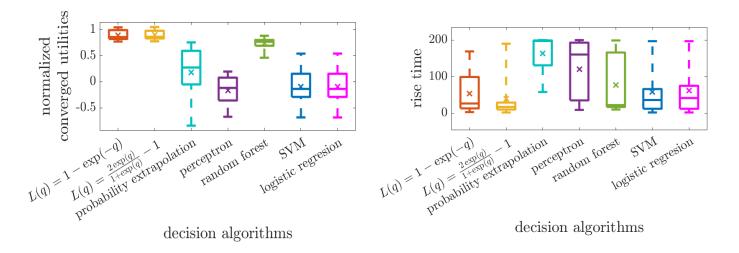
- Systematically trade-off exploration vs. exploitation
- Immediate feedback from small samples toward better policy
- Ability
- to add new features
- Convergence
 - to optimal parameters
- Continuously adapt to changes

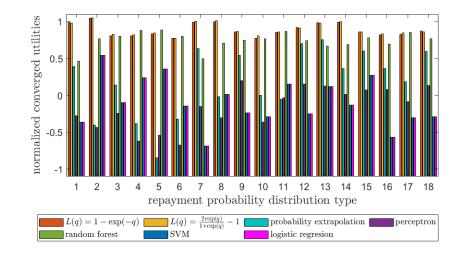
Microfinance from a control perspective

1. Robustness against missing data



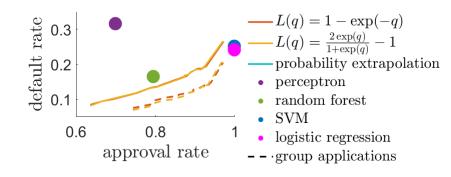
2. Ability to deal with diverse microfinance distributions



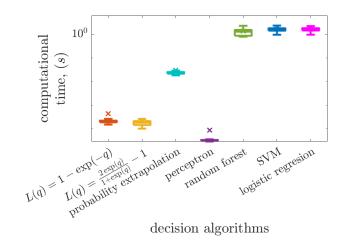


Microfinance from a control perspective

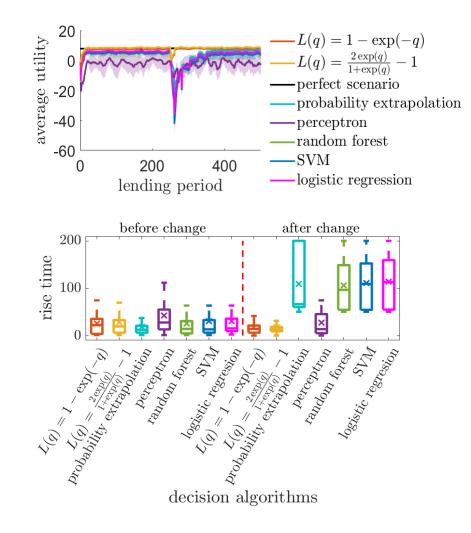
3. Tradeoff between default rate vs. approval rate



4. Cheaper computational cost



5. Adaptation to changes



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Constraints vs robust performance in human

